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EDITED BY  
Miha Ravnik,  
University of Ljubljana, Slovenia

REVIEWED BY  
Nektarios Papadogiannis,  
Hellenic Mediterranean University,  
Greece  
Laura Cattaneo,  
Max Planck Institute for Nuclear Physics,  
Germany

\*CORRESPONDENCE  
Milutin Kovačev,  
kovacev@iqo.uni-hannover.de

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# High-order harmonic spectroscopy in an ionized high-density target

Heiko G. Kurz<sup>1</sup>, Martin Kretschmar<sup>2</sup>, Thomas Binhammer<sup>3</sup>,  
Tamas Nagy<sup>2</sup>, Detlev Ristau<sup>1,4,5</sup>, Manfred Lein<sup>6</sup>,  
Uwe Morgner<sup>1,4,5</sup> and Milutin Kovačev<sup>1,4\*</sup>

<sup>1</sup>Leibniz Universität Hannover, Institut für Quantenoptik, Hannover, Germany, <sup>2</sup>Max Born Institute, Berlin, Germany, <sup>3</sup>NeoLase GmbH, Hannover, Germany, <sup>4</sup>Cluster of Excellence PhoenixD (Photonics, Optics and Engineering-Innovation Across Disciplines, Hannover, Germany, <sup>5</sup>Laser Zentrum Hannover e.V., Hannover, Germany, <sup>6</sup>Leibniz Universität Hannover, Institut für Theoretische Physik, Hannover, Germany

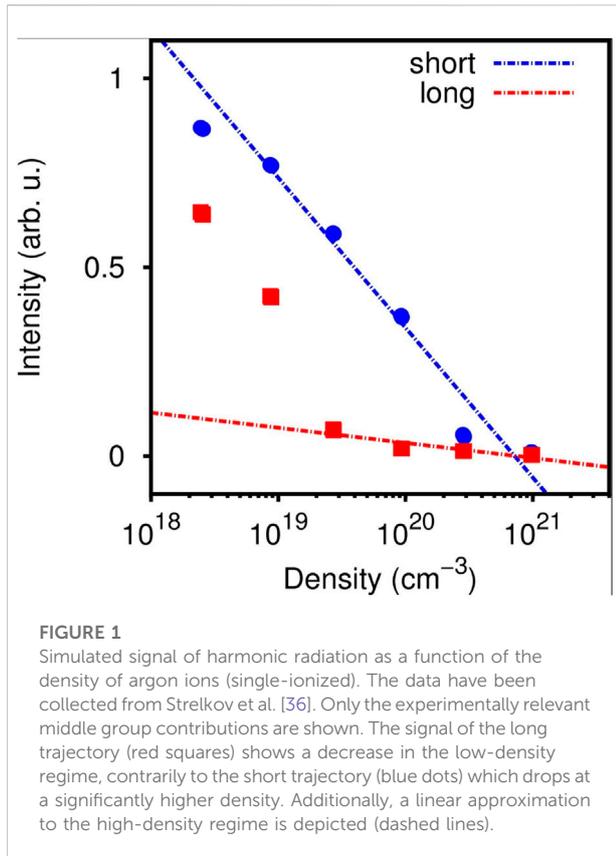
We use high-order harmonic spectroscopy to study ionization dynamics in a macroscopic target with tunable density, spanning over six orders of magnitude. In an *in situ* pump-probe experiment, the target is prepared at different densities with varying degrees of laser-induced ionization. High-order harmonic radiation is generated in the pre-ionized target, and a steepening in the decrease of the harmonic yield is observed for increasing pre-ionization, allowing not only to identify the contributing quantum paths during high-order harmonic generation but also in determining the amount of ionization within the target. The measurements allow probing of ionization dynamics in laser-induced plasma with high spatio-temporal resolution and are specifically of interest for the optimization of the harmonic generation process in high-density targets with number densities of up to  $10^{22}$  cm<sup>-3</sup>.

## KEYWORDS

high-order harmonic generation, spectroscopy, ionization, droplets, water, pump-probe, high-density target

## Introduction

High-order harmonic generation (HHG) [1] requires laser intensities comparable to the inner atomic electric fields in order to induce tunnel ionization [2, 3]. These intensities are typically within the range from  $I \approx 10^{13}$  to  $10^{15}$  W/cm<sup>2</sup>. However, by applying strong electric fields onto a macroscopic ensemble the target's composition is affected, changing it from usually being purely neutral into a mixture of neutral particles, ions, and free electrons which can severely influence the HHG process. The presence of free electrons, for example, may shift the phase-matching conditions by inducing an additional phase term *via* a change in the refractive index, deteriorating the conversion efficiency [4, 5]. Furthermore, the fast variation of the electron density during the driver pulse leads to transient phase-matching conditions, which may result in blue-shifting or spectral broadening of the harmonic radiation [6–9]. Much effort has been carried



out in order to minimize the plasma effects on HHG, searching for optimum conditions for the nonlinear frequency conversion [10–18, 20].

However, plasma formation not only has negative impacts on HHG but it also opens possibilities for the generation of extreme ultraviolet radiation that differs from conventional gas targets, such as wakefield acceleration [20] or HHG from relativistic oscillating mirrors [25, 24, 23, 21]. Even methods for the spatial separation of different spectral components of harmonic radiation during the HHG process have been applied [25]. The plasma itself can also be used as a medium for HHG, enhancing the emission process at the whole, as in the case of laser-ablated plasmas as the target medium [28, 26]. Furthermore, plasmas give rise to amplify single-harmonic orders through atomic [33, 32, 31, 30, 28] or fano-shaped resonances [33].

Additional benefits arise from a pre-ionized target with a low free electron density, where the source of HHG no longer lies within the neutral particle but in the ion. Within these ionic targets, enhancing the harmonic cutoff becomes accessible due to the higher ionic potential [36, 34]. The range of an ionic Coulomb potential, however, is large compared with the short-ranged character of a neutral atom so that the effect of neighboring ions on the electron along its excursion in the continuum is not negligible. An ionic background medium,

therefore, provides a source of perturbation for electronic trajectories during HHG, where the electron is deflected by neighboring ions within the target and misses its parent ion so that the recombination step is inhibited.

In a theoretical work, V. Strelkov et al. [36] simulated the emission of harmonic radiation from a neutral argon atom surrounded by an ionized background medium in order to study the influence of neighboring ions on the emission process. The numerical calculations were performed for the single-atom response, considering a single-ionized target. Figure 1 depicts the calculated yield of harmonic orders in the plateau region from [36] for an intensity of a driving pulse of  $I_{\text{pump}} = 2 \times 10^{14} \text{ W/cm}^2$  and an ionized background medium. The pulse duration has been set to 50 fs at a wavelength of 800 nm. The contributions of short (blue circles) and long (red squares) trajectories have been distinguished in the calculations due to the fact that the emission *via* the two quantum paths features a severe difference in the slope as the target's density increases. Although the signal originating from the short trajectories is less affected by surrounding ions, particularly for densities with  $\rho < 10^{19} \text{ cm}^{-3}$ , the contribution *via* the long trajectory decreases rapidly. The origin of the trajectory-dependent emitted harmonic yield lies in the inequality of excursion times  $\tau_{\text{ex}}$  between the two quantum paths [4, 38–40]. Since the long trajectory has a larger excursion time, the electron wavepacket is spreading more severely, thus accumulating a higher phase contribution induced by the long-ranging Coulomb potential of neighboring ions [36]. Increasing the density of the ionized medium, therefore, leads to larger distortions, and the effect of separation becomes pronounced. Both contributions, however, feature a linear decrease in the high-density regime (dashed lines in Figure 1), where the slopes are well distinguishable. Additionally, the calculations by V. Strelkov et al. indicate that the difference between the slopes decreases as the medium becomes less ionized, approaching the same intermediate value for a neutral medium.

Detecting these microscopic effects in a macroscopic ensemble, however, is nontrivial not only because the amount of ionization in the target has to be controlled but also following the deflection of electronic trajectories is challenging as well. Moreover, the density regime where the linear dependence of the harmonic yield becomes observable is beyond  $\rho > 2 \times 10^{19} \text{ cm}^{-3}$ , exceeding the available density supported by conventional setups such as gas jets or gas cells, resulting in a need for a high-density target to observe these effects. In order to match the experimental requirements of a high-density target in this work, we apply a liquid–water droplet in a vacuum as a target for HHG in an *in situ* pump-probe setup [45, 44, 43, 42, 40], giving access to densities of up to  $\rho_0 = 3.34 \times 10^{22} \text{ cm}^{-3}$ . Our approach is complemented by making use of high-order harmonic spectroscopy which is capable of observing the electronic motion and its dynamic interaction with strong laser fields with unprecedented precision since the information is imprinted onto the emitted radiation in an *in situ* process [52,

51, 50, 49, 48, 47, 45]. Our observations demonstrate ionization dynamics which allow for estimates on the degree of ionization of the target medium. These measurements, therefore, contribute to the optimization of high-harmonic generation in high-density targets which have been investigated recently [18, 19, 45].

## Materials and methods

Two time-delayed, intense laser pulses with a duration of 40 fs and variable energy of up to 1 mJ each are focused collinearly by the same lens ( $f = 500$  mm) reaching a size in the focal region of about 90 microns in diameter. Intensity control is realized *via* attenuation through the combination of two thin-film polarizers in reflection and a half-wave plate in each arm. The droplets are prepared by using a capillary nozzle containing a piezoelectric aperture in order to induce hydrodynamic instability for a controlled water jet breakup. The deterministic series of water droplets are characterized *via* imaging to a diameter of about  $15 \mu\text{m}$  [44, 42]. The droplet is expanded by the pump pulse through a laser-induced optical breakdown (LIB) [53–55], initiating a rapid decrease in its density but not contributing to HHG due to the high initial density and the ps-scale delay in the expansion [54, 56]. An additional tuning of the pump pulse intensity allows in controlling the laser-induced ionization. Hence, a target can be generated whose composition reaches from consisting mainly of neutral particles to being dominated by ions, controlled by the intensity of the pump pulse. Depending on the time delay  $t$ , which reaches from 0 ns to 15 ns, different target densities become accessible for HHG with the probe pulse, and the droplet's internal composition can be studied *in situ via* high-order harmonic spectroscopy. It should be noted that the derived density calculations depend on the water droplet expansion upon LIB by the pump pulse. The estimates take into account the ionic mass, the ionization potential, and the density of liquid water.

The high-order harmonic spectra have been recorded as a function of the pump-probe time delay and the intensity of the pump pulse using an XUV grazing-incidence spectrometer (LHT 30, Horiba-Jobin-Yvon, 500 lines/mm) with an attached micro-channel plate. A model from plasma physics [57] describing the ion velocities is used to derive the mapping of the delay  $t$  onto the density evolution  $\rho(t, I_{\text{pump}})$ , where  $I_{\text{pump}}$  is the intensity of the pump pulse. Assuming a uniform expansion of the target, which is justified for  $t > 200\text{ps}$ , allows us to calculate the volume of the droplet as a function of time.

$$V(t, I) = \frac{4}{3} \pi (r_0 + \bar{v}_{\text{ion}}(I) \cdot t)^3, \quad (1)$$

where  $\bar{v}_{\text{ion}}(I)$  is the ion velocity,  $r_0$  is the initial radius of the droplet, and  $t$  denotes the pump-probe delay. By computing the relative change of the target's volume

$$\Delta V(t, I) = \frac{V(t, I)}{V_0} \quad (2)$$

with the volume at time zero  $V_0 = V(0, I)$  and applying the density of liquid water  $\rho_0 = 3.35 \times 10^{22} \text{cm}^{-3}$ , this gives access to the density evolution of the target as a function of time and intensity [42].

$$\begin{aligned} \rho(t, I) &= \frac{\rho_0}{\Delta V(t, I)} \\ &= \rho_0 V_0 / \\ &\quad \times \left\{ \frac{4}{3} \pi \left( r_0 + \frac{1}{\sqrt{3} \cdot M} \cdot \sqrt{5 \cdot Z \alpha^{-3} \left( \frac{3}{50} M C r_0 \right)^{\frac{2}{3}} \cdot t \cdot \beta(\tau) \cdot I^{\frac{2}{3}}} \right)^3 \right\}. \end{aligned} \quad (3)$$

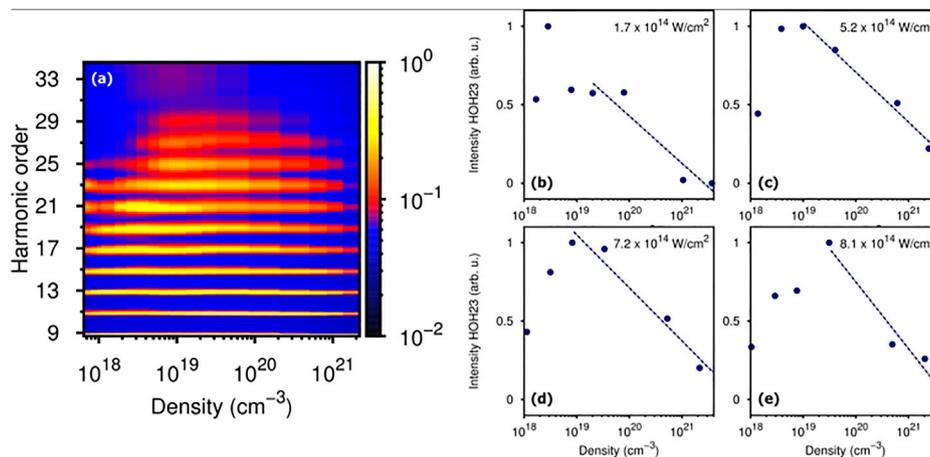
Here,  $M$  denotes the ionic mass,  $Z$  the degree of ionization (set to be  $Z = 1$ ),  $\alpha = (Z + 1)/Z$ ,  $I$  the intensity of the laser pulse, and  $C$  is calculated according to [57]. The parameter  $\beta(\tau)$  is determined experimentally and takes the influence of the pulse duration  $\tau$  on the LIB process into account. As a result, the harmonic yield is obtained as a function of the density [43]. By placing the focus before the droplet with respect to the propagation direction, the short trajectory is selected *via* phase matching [4, 43, 58].

## Experimental results and discussion

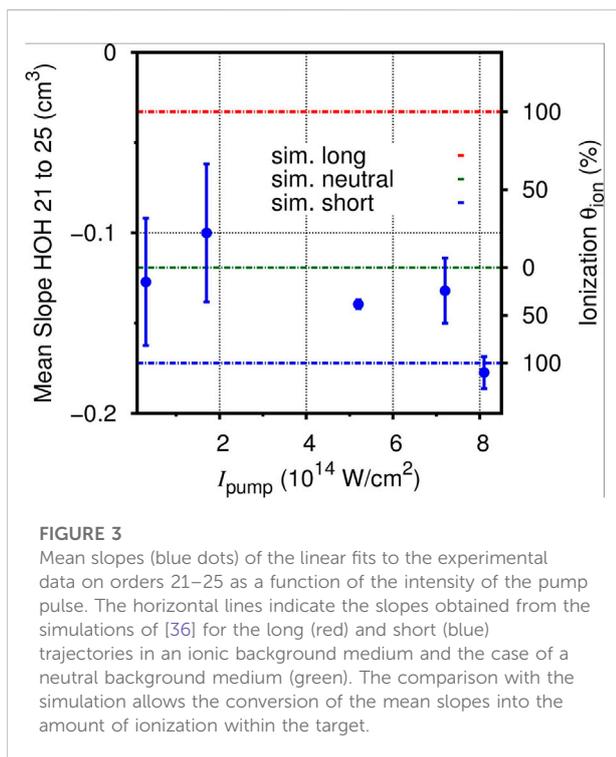
Figure 2A depicts the harmonic spectrum as a function of the density evolution of the target for intensities of the pump- and probe-pulse of  $I_{\text{pump}} = 7.2 \times 10^{14} \text{W/cm}^2$  and  $I_{\text{probe}} = 9.5 \times 10^{14} \text{W/cm}^2$ , respectively. The signal increases toward a maximum around a density of  $\rho \approx 10^{19} \text{cm}^{-3}$ , where optimum conversion efficiencies for higher orders are also observed. Further increase in the density results in a decreasing signal.

For more detailed insights into the density-dependent evolution of the harmonic yield and to study the influence of ionization on the HHG process, Figures 2B–E show outlines of the 23rd harmonic order's yield (blue dots) for different intensities of the pump pulse. The signal increases for all intensities as a function of the density due to the larger number of emitters contributing to HHG until a maximum of around  $\rho \approx 10^{19} \text{cm}^{-3}$  is reached. From there on, the high-density regime is reached and the signal drops. The blue-dashed line indicates the linear fit to the high-density regime, where a steepening in the slope is observed with the increasing intensity of the pump pulse.

The decreasing signal in the high-density regime in Figures 2B–E can be attributed to a perturbation of the electron on its excursion in the continuum, which is induced by adjacent particles. Since the mean inter-particle distance in the target is reduced as the density is increased, approaching the maximum electronic displacement during HHG, the possibility for a perturbation of electronic trajectories by neighboring particles



**FIGURE 2** (A) Measured spectra of harmonic radiation as a function of the density of the target at an intensity of the pump pulse of  $I_{\text{pump}} = 7.2 \times 10^{14}$   $\text{W/cm}^2$  and an intensity of the probe pulse of  $I_{\text{probe}} = 9.5 \times 10^{14}$   $\text{W/cm}^2$ . (B) to (E) outlines the signal of the 23rd harmonic order with different intensities of the pump pulse. The dashed lines indicate the linear fit to the high-density regime. The slopes of the fits decrease from (B)  $-0.131$  via (C)  $-0.138$  and (D)  $-0.147$  to (E)  $-0.185$ .



**FIGURE 3** Mean slopes (blue dots) of the linear fits to the experimental data on orders 21–25 as a function of the intensity of the pump pulse. The horizontal lines indicate the slopes obtained from the simulations of [36] for the long (red) and short (blue) trajectories in an ionic background medium and the case of a neutral background medium (green). The comparison with the simulation allows the conversion of the mean slopes into the amount of ionization within the target.

increases, suppressing the harmonic yield [43]. However, the steepening of the linear fit’s slope as a function of the pump pulse’s intensity is observed, indicating that an additional change in the composition of the target medium is induced. At higher pump intensities, a larger fraction of the molecules within the droplet is ionized [55, 59–61], providing a long-ranging ionic

Coulomb field. When the probe pulse interacts with the prepared target to drive the HHG process, the electrons are not only perturbed along their trajectories by neutral particles but also experience an additional deflection by the ionic Coulomb fields. Consequently, the recombination step is perturbed even more and the harmonic yield decreases; the more rapid, the higher the number of ions induced by the pump pulse is within the target, resulting in a steepening of the slope in the high-density regime.

The inherent sensitivity of the HHG process to the presence of residing ions in the high-density regime enables us to elucidate the ionization dynamics explaining the behavior of the target in terms of generation efficiency within the macroscopic ensemble by analyzing the slope of the harmonic signal. To this end, Figure 3 compares the slope of the harmonic signal versus the pump intensity, averaged over the orders 21–25, with the calculations by V. Strelkov et al. [36] for an ionized (dashed blue line for the short trajectory and dashed red line for the long trajectory) and a neutral background medium (dashed green line). In the latter case, the slopes of long and short trajectories are non-distinguishable and, therefore, deliver a single, intermediate value. At low intensities, the mean slopes are close to the calculated value for a neutral medium, which suggests that the target’s composition is dominated by neutral particles. It should be noted that data for the lower intensity of the pump pulse are close to the threshold intensity for LIB such that the expansion process of the droplet may differ from the model used previously. The mean slope becomes more negative as a function of  $I_{\text{pump}}$ , resulting in a better agreement between the measurement and the simulation for the short trajectory. Considering that the short trajectory has been selected in the experiment, the convergence of the measurement toward the

theoretical value is consistent with the assumption that a larger amount of ionization is induced by the pump pulse, affecting the HHG process.

Considering that the ionization fraction in the simulation of a neutral background is 0% (dashed green line in Figure 3), while it is 100% for the value of the short trajectory (dashed blue line in Figure 3), the measurements deliver a degree of ionization reaching from  $\theta_{\text{ion}} < 10\%$  to  $\theta_{\text{ion}} \approx 100\%$ , indicating that the target can be prepared in different extents of ionization. Additionally, the measurement's convergence toward the theoretical prediction of the short trajectory confirms that the long trajectory can be neglected (dashed red line in Figure 3) since the short quantum path has been selected in the experiment. The intensity of the probe pulse, however, is high enough to lead to additional ionization within the target; otherwise, no harmonic radiation would be emitted. A contribution of the HHG driving pulse to  $\theta_{\text{ion}}$ , therefore, has to be considered. Its impact on the measurement is estimated by a comparison with experimental pump-probe results of LIB in water using low-intensity probe pulses that do not lead to further ionization.

A measurement by Sarpe-Tudoran et al. [56] applied two 35 fs pulses with 780 nm to a water jet. The pump intensity was set to 1.5 times the threshold intensity for LIB ( $I_{\text{LIB}} \approx 1.4 \times 10^{14} \text{ W/cm}^2$ ). Its result is an ionization degree of  $\theta_{\text{ion}} \approx 3.6\%$ . A comparable experiment by Brown et al. [55] indicated an ionization fraction of  $\theta_{\text{ion}} \approx 6\%$ . Both results are in reasonable agreement with our findings in Figure 3. Hence, we deduce that although the probe pulse is intense enough to induce severe ionization, the generated ions are screened by their associated electrons, resulting in no additional perturbation of other molecules generating harmonic radiation. This shows that *in situ* high-order harmonic spectroscopy is able to map laser-induced ionization dynamics important for the understanding of generation efficiencies in macroscopic targets.

## Conclusion

Using liquid water droplets in an *in situ* pump-probe experiment, we have demonstrated the influence of a pre-ionized target on the HHG process. The density of the target was decreased using an intense pump pulse which triggers a laser-induced-breakdown-based expansion. Additionally, the amount of laser-induced ionization within the target was controlled *via* the intensity of the pump pulse. The harmonic radiation was generated in the pre-ionized target by applying a second, time-delayed probe pulse. Our findings indicate that an ionic background medium can severely distort the electron along its excursion in the continuum and, thus, verify the theoretical prediction by V. Strelkov et al. [36]. We have shown that ionization induced by the pump pulse can be a major

contribution for the distortion of electronic trajectories and is able to significantly reduce the conversion efficiency of HHG. Moreover, by applying different intensities of the pump pulse, we show laser-induced ionization dynamics allowing estimates on the harmonic generation efficiency within the target by high-order harmonic spectroscopy. Our measurements open new routes to probe ionization dynamics in laser-induced plasmas with high spatio-temporal resolution and are specifically of interest for the optimization of the HHG process in high-density targets [33, 32, 31, 30, 29, 62, 28, 26].

## Data availability statement

The original contributions presented in the study are included in the article/Supplementary Material; further inquiries can be directed to the corresponding author.

## Author contributions

The authors contributed to manuscript writing (HK, MaKr, ML, and MiKo) and editing (TB, TN, DR, and UM).

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## Conflict of interest

Author TB is employed by NeoLASE GmbH.

The remaining authors declare that the research was conducted in the absence of any commercial or financial relationships that could be construed as a potential conflict of interest.

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